

CHE323/CHE384
Chemical Processes for Micro- and Nanofabrication

Formulas Lectures 1-19

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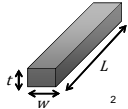
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Doping, Conductivity, Resistance

- Doping charge balance: $N_D^+ + p = N_A^- + n$
- Mass action equation: $np = n_i^2$
 N_A = acceptor concentration N_D^+ = ionized donor concentration
 N_D = donor concentration n = mobile electron concentration
 N_A^- = ionized acceptor conc. p = mobile hole concentration
- Resistivity and conductivity:
 $\frac{1}{\rho} = \sigma = q(n\mu_n + p\mu_p)$ Resistance $R = \rho \frac{L}{A}$, $A = wt$
Sheet Resistance $R_s = \rho/t$

q = charge on electron = 1.6×10^{-19} C
 μ_n = electron mobility = $1500 \text{ cm}^2/\text{Vs}$ for Si at 300K
 μ_p = hole mobility = $450 \text{ cm}^2/\text{Vs}$ for Si at 300K
 $n_i = 1.5 \times 10^{10} \text{ cm}^{-3}$ for Si at 300K



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P-N Junction

- Built-in voltage (V_0) and the depletion width (W)

$$V_0 = \frac{kT}{q} \ln \left(\frac{N_A N_D}{n_i^2} \right) \quad W = \sqrt{\frac{2\epsilon_{Si}(V_0 - V)}{q} \left(\frac{1}{N_A} + \frac{1}{N_D} \right)} + \frac{V}{E_{field}}$$

$$\epsilon_{Si} = 11.7\epsilon_0, \quad \epsilon_0 = 8.8542 \times 10^{-12} \text{ C/Vm} \quad \text{At } T = 300 \text{ K}, \quad \frac{kT}{q} = 25 \text{ mV}$$
- Diode Equation: current $I_{diode} = I_0 (e^{qV/kT} - 1)$
- Capacitance: $C_{p-n, junction} = \frac{\epsilon A}{W} = A \sqrt{\frac{q\epsilon_{Si}}{2(V_0 - V)} \left(\frac{N_D N_A}{N_D + N_A} \right)}$

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Deal-Grove Oxidation Model

$$t_{ox}^2 + At_{ox} = B(t + \tau) \quad \tau = \frac{t_o^2 + At_o}{B}$$

TABLE 4.1 / OXIDATION COEFFICIENTS FOR SILICON (111) wafers

Temperature (°C)	Dry			Wet (640 torr)	
	A (μm)	B (μm ² /hr)	τ (hr)	A (μm)	B (μm ² /hr)
800	0.370	0.0011	9	—	—
920	0.235	0.0049	1.4	0.50	0.203
1000	0.165	0.0117	0.37	0.226	0.287
1100	0.090	0.027	0.076	0.11	0.510
1200	0.040	0.045	0.027	0.05	0.720

The τ parameter is used to compensate for the rapid growth regime for thin oxides (after Deal and Grove).
 For (100) wafers, multiply A by 1.68.

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Deal-Grove Temperature Dependence

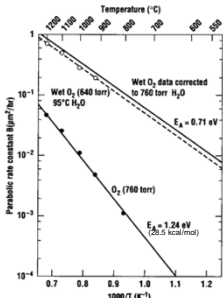


Figure 4.2 Arrhenius plot of the B oxidation coefficient. The wet parameters depend on the H₂O concentration and therefore on the gas flows and pyrolysis conditions (after Deal and Grove). (11) wafers

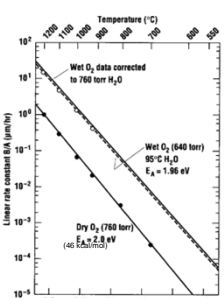


Figure 4.3 Arrhenius plot of the ratio (B/A) of the oxidation parameters (after Deal and Grove). (11) wafers

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Diffusion Review

- Fick's 2nd law of Diffusion (in 1-D):

$$\frac{\partial C(x, t)}{\partial t} = \frac{\partial}{\partial x} \left(D \frac{\partial C(x, t)}{\partial x} \right)$$
- In 3-D: $\frac{\partial C}{\partial t} = \nabla(D\nabla C)$, $\nabla = \frac{\partial}{\partial x} + \frac{\partial}{\partial y} + \frac{\partial}{\partial z}$
- Analytical solutions are for $D = \text{constant}$ and certain special boundary conditions
- Electric field enhancement: $\eta \approx \frac{C(z)}{\sqrt{C^2(z) + 4n_i^2}}$
 $D_{enhanced} = D(1 + \eta)$

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Diffusion Case 1: Constant Source

- Initial and boundary conditions
 - $C(0,t) = C_s$ (concentration at top is constant)
 - $C(z,0) = 0$ for $z > 0$ (initial condition)
 - $C(\infty,t) = 0$

- Solution: $C(z,t) = C_s \operatorname{erfc}\left(\frac{z}{2\sqrt{Dt}}\right)$, $t > 0$
 \sqrt{Dt} = diffusion length (average distance a dopant moves)

$$Q_T(t) = \int_0^\infty C(z,t) dz = \frac{2}{\sqrt{\pi}} C_s \sqrt{Dt}$$

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Diffusion Case 2: Limited Source (drive-in diffusion)

- Initial and boundary conditions
 - $C(z,0) = 0$, $z > 0$
 - $dC(0,t)/dt = 0$ (no flux at top)
 - $C(\infty,t) = 0$
 - Constant dose: $\int_0^\infty C(z,t) dz = Q_T = \text{constant}$

- Solution:

$$C(z,t) = \frac{Q_T}{\sqrt{\pi Dt}} e^{-z^2/4Dt}, \quad t > 0$$

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Case 3: Buried Gaussian Source

- Initial and boundary conditions
 - Gaussian: $C(z,0) = \frac{Q_T}{\sqrt{2\pi\sigma_0^2}} e^{-(z-\mu)^2/2\sigma_0^2}$, $z \geq 0, \mu \gg \sigma_0$
 - $dC(0,t)/dt = 0$ (no flux at top)
 - $C(\infty,t) = 0$
- Solution: $\sigma^2 = \sigma_0^2 + 2Dt$ ($\sqrt{2Dt}$ = diffusion length)

$$C(z,t) = \frac{Q_T}{\sqrt{2\pi\sigma^2}} e^{-(z-\mu)^2/2\sigma^2}, \quad z \geq 0, t \geq 0$$

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Gaussian Ion Implantation Model

- Gaussian model for the distribution of dopants
 - Mean = R_p = projected range
 - Standard deviation = ΔR_p = straggle
 - Dose = ϕ (# dopants/cm²)

$$N(x) = \frac{\phi}{\sqrt{2\pi}\Delta R_p} e^{-(x-R_p)^2/2\Delta R_p^2}$$

- Lateral scattering
 - For As, Sb: $\Delta R_\perp \approx \Delta R_p$
 - For P: $\Delta R_\perp \approx 1.2\Delta R_p$
 - For B: $\Delta R_\perp \approx 2\Delta R_p$

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Ion Implantation Model Parameters

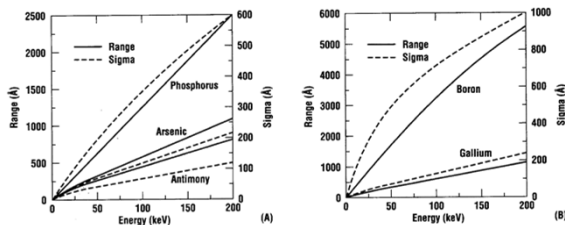


Figure 5.9 Projected range (solid lines and left axis) and standard deviation (dashed lines and right axis) for (A) n-type, (B) p-type, and (C) other species into a silicon substrate; (D) n-type and (E) p-type dopants into a GaAs substrate; and several implants into (F) SiO₂ and (G) AZ111 photoresist (data from Gibbons et al.).

$$\Delta R_p \approx \frac{2}{3} R_p \left(\frac{\sqrt{M_i M_t}}{M_i + M_t} \right) \quad \begin{matrix} i = \text{ion}, t = \text{target} \\ M = \text{atomic mass} \end{matrix}$$

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Thermal Transfer Mechanisms

- Radiative: Stefan-Boltzmann equation

$$\text{Heat Flow} = \dot{q} = \epsilon \sigma T^4$$

ϵ = emissivity of emitting body ($\epsilon = 1$ for black body)
 σ = Stefan-Boltzmann Constant = $5.6697 \times 10^{-8} \text{ W/m}^2\text{-K}^4$

- Conduction: $\dot{q} = k\nabla T$
- Convection: $\dot{q} = h(T - T_\infty)$

$$\epsilon(\lambda) = 1 - R(\lambda) - T(\lambda)$$

$$\epsilon_{Si} \approx 0.7, \quad T_{Si} \approx 0$$

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