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CHE323/CHE384  
Chemical Processes for Micro- and Nanofabrication

## Formulas Lectures 20-37

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## Mean Free Path

- Mean free path ( $\lambda$ ) = average distance a molecule travels between collisions

$$\lambda = \frac{kT}{\sqrt{2}\pi P d^2}$$

Boltzmann Constant  $kT$  Absolute Temperature of Chamber (not vapor)  
Pressure  $P$  Gas molecule diameter (2-5Å)

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## Evaporation

Single Wafer Geometry

view factor =  $\cos\theta$   
Surface area  $\propto r^2$   
view factor =  $\cos\theta$

$$rate \propto \frac{\cos^2\theta}{r^2} = \frac{h^2}{(h^2 + x^2)^2}$$

Multiple Wafer Geometry

view factor =  $\cos\theta$

$$rate \propto \frac{\cos^2\theta}{h^2} \quad \cos\theta = \frac{h/2}{r_0}$$

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## CVD Deposition Rate

$$v = \frac{k_T}{N} C_g = \frac{k_T}{N} \left(\frac{1}{kT}\right) P_g \quad k_T = \frac{h_g k_s}{h_g + k_s}$$

$$D_g \propto T^{\frac{3}{2}} \frac{P_g}{P_T}, \quad \delta \text{ varies slowly with } T$$

$D_g$  = diffusivity of reactant in gas  
 $C_g$  = bulk reactant concentration  
 $\delta$  = boundary layer thickness  
 $h_g = D_g/\delta$  = mass transfer coefficient  
 $k_s$  = reaction rate constant  
 $N$  = # atoms/cm<sup>3</sup> in deposited film

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## RC Time Constant

Interlevel

$\epsilon_{ox} = K_{ox} \epsilon_o$   
 $R = \rho_m \frac{L}{wt_m}$      $C = \epsilon_{ox} \frac{wL}{t_{ox}}$   
 $\tau = RC = \rho_m \epsilon_{ox} \frac{L^2}{t_m t_{ox}}$

$\rho_{AL} = 2.8 \times 10^{-6} \Omega \text{ cm}$ ,  $\rho_{Cu} = 1.7 \times 10^{-6} \Omega \text{ cm}$ , for  $\text{SiO}_2$   $K_{ox} = 3.9$

Intralevel

$R = \rho_m \frac{L}{w_s t_m}$      $C = \epsilon_{ox} \frac{t_m L}{w_s}$   
 $\tau = RC = \rho_m \epsilon_{ox} \frac{L^2}{w_s t_m}$

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## Defect Model

- Independent defects:  $Y = (1 - G)e^{-A_c D_o}$   
 $G$  = fraction of die that always fail (edge die)  
 $A_c$  = critical area (area of die where a defect matters)  
 $D_o$  = defect density (# killer defects/area)

### Main Western Electric Rules

- Any single point falls outside of the +/- 3 $\sigma$  limits
- Eight successive points are above the mean, or eight successive points are below the mean
- Two out of three successive points are between 2 $\sigma$  and 3 $\sigma$ , or between -2 $\sigma$  and -3 $\sigma$
- Four out of five successive points are between 1 $\sigma$  and 3 $\sigma$ , or between -1 $\sigma$  and -3 $\sigma$

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### Process Capability Index: $C_p$ and $C_{pk}$

$$C_p = \frac{USL - LSL}{6\sigma} \quad \begin{array}{l} USL = \text{upper spec limit} \\ LSL = \text{lower spec limit} \end{array}$$

$$C_{pk} = (1 - k)C_p \quad k = \frac{2|Target - mea|}{USL - LSL}$$

- $C_{pk} > 1$  is minimum requirement
- $C_{pk} > 1.5$  is good
- $C_{pk} > 2$  is great (called "six-sigma" quality)

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### Etch and CMP

- Etch Selectivity
  - Selectivity versus mask material ( $s = r_{SiO_2}/r_{resist}$ )
  - Selectivity versus etch stop layer ( $s = r_{SiO_2}/r_{Si}$ )

$$\text{Anisotropy} = 1 - \frac{r_H}{r_V}$$

$$\text{CMP Polish Rate} \propto vP \quad \begin{array}{l} v = \text{relative speed} \\ P = \text{pressure} \end{array}$$

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### Useful Constants

- Avogadro Constant  $6.02204 \times 10^{23} \text{ mole}^{-1}$
- Boltzmann Constant ( $k$ )  $1.38066 \times 10^{-23} \text{ J/K}$   
 $8.617 \times 10^{-5} \text{ eV/K}$   
 $1.3626 \times 10^{-22} \text{ atm-cm}^3/\text{K}$
- Gas Constant ( $R$ )  $1.987 \text{ cal/mole/K}$
- Electric Charge ( $q$ )  $1.60218 \times 10^{-19} \text{ C}$
- Permittivity in vacuum ( $\epsilon_0$ )  $8.854 \times 10^{-14} \text{ F/cm}$
- Thermal voltage at 300 K ( $kT/q$ )  $0.0259 \text{ V}$
- **Pressure:**  $1 \text{ atm} = 1.01325 \times 10^5 \text{ Pa} = 1.01325 \text{ bar} = 760 \text{ torr} = 14.696 \text{ psi}$  ( $1 \text{ Pa} = 1 \text{ kg}/(\text{m} \cdot \text{s}^2) = 1 \text{ N}/\text{m}^2$ )
- **Energy:**  $1 \text{ J} = 1 \text{ kg m}^2/\text{s}^2 = 9.4782 \times 10^{-4} \text{ Btu} = 6.2415 \times 10^{16} \text{ eV} = 0.23901 \text{ cal} = 1 \text{ A V s}$
- **Capacitance:**  $1 \text{ F} = 1 \text{ A s/V} = 1 \text{ C/V} = 1 \text{ s/W}$

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