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WHAT STARTS HERE CHANGES THE WORLD

CHE323/CHE384
Chemical Processes for Micro- and Nanofabrication

Lecture 5 Doping

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Doping

- **Doping:** intentionally adding impurities into the crystal structure to change n (mobile electron concentration) and p (mobile hole concentration) to be different from n_i
 - Intrinsic material: undoped, pure
 - Extrinsic material: doped semiconductor

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Two Types of Dopants

Acceptors Donors

Group III V

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Intrinsic Silicon

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Donor (Group V) Impurity

- Donors have five electrons in their outer shell
- When the impurity is activated (incorporated into the crystal lattice), it has one unbonded electron
- This electron is easily removed at room temperature, resulting in an ionized dopant atom and a free electron

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Acceptor (Group III) Impurity

- Acceptors have three electrons in their outer shell
- When the impurity is activated (incorporated into the crystal lattice), it needs one more electron to complete its bonds
- This electron is easily supplied by a nearby bond at room temperature, resulting in an ionized dopant atom and a mobile hole

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Doping - The Math

- Charge balance: $N_D^+ + p = N_A^- + n$
- Mass action equation: $np = n_i^2$

$N_A = \text{acceptor concentration}$	$n = \text{mobile electron concentration}$
$N_D = \text{donor concentration}$	$p = \text{mobile hole concentration}$
$N_A^- = \text{ionized acceptor conc.}$	
$N_D^+ = \text{ionized donor conc.}$	

- At room temperature, $N_A^- \approx N_A$, $N_D^+ \approx N_D$

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The Math – an example

- Consider a wafer that is doped p-type, with $N_A = 2 \times 10^{16} \text{ cm}^{-3}$.
- Now, add n-type dopant with $N_D = 1 \times 10^{18} \text{ cm}^{-3}$. What are n and p (at room temp.)?
- Assume complete ionization: $N_A \approx N_A^-$, $N_D \approx N_D^+$
- Solve simultaneous equations:

$$np = n_i^2 \qquad N_D^+ + p = N_A^- + n$$

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The Math – an example (2)

- Simplification: since $N_D \gg N_A$, we will have lots of mobile electrons (majority carrier) and not many holes (minority carrier)

$$N_D^+ + p = N_A^- + n \rightarrow n \approx N_D - N_A = 9.8 \times 10^{17} \text{ cm}^{-3}$$

small

$$p = \frac{n_i^2}{n} = \frac{(1.5 \times 10^{10} \text{ cm}^{-3})^2}{9.8 \times 10^{17} \text{ cm}^{-3}} = 2.3 \times 10^2 \text{ cm}^{-3}$$

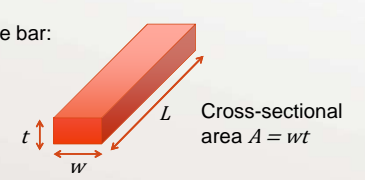
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Metal/Insulator Resistor

- Conductivity (σ) and resistivity ($\rho = 1/\sigma$) are material properties

Resistance of the bar:

$$R = \rho \frac{L}{A}$$


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Semiconductor Resistor

- Conductivity of a semiconductor can be varied by doping

$$\sigma = q(n\mu_n + p\mu_p)$$

$q = \text{charge on electron} = 1.6 \times 10^{-19} \text{ C}$
 $\mu_n = \text{electron mobility} = 1500 \text{ cm}^2/\text{Vs}$ for Si at 300K
 $\mu_p = \text{hole mobility} = 450 \text{ cm}^2/\text{Vs}$ for Si at 300K

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Semiconductor Resistor

- A wafer that is doped p-type, with $N_A = 2 \times 10^{16} \text{ cm}^{-3}$. Now, add n-type dopant with $N_D = 1 \times 10^{18} \text{ cm}^{-3}$ in the region where we want our resistor.

$$\sigma_{\text{wafer}} = q(n\mu_n + p\mu_p) \approx qN_A\mu_p = 1.44 (\Omega\text{cm})^{-1}$$

[Units: 1 C/s = 1 A (amperes), 1 V/A = 1 Ω (ohm)]

$$\sigma_{\text{resistor}} = q(n\mu_n + p\mu_p) \approx qN_D\mu_n = 240 (\Omega\text{cm})^{-1}$$

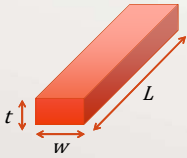
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Semiconductor Resistor

- Let our doping occur in a confined region, with $L = 2 \mu\text{m}$, $w = 0.25 \mu\text{m}$, $t = 0.12 \mu\text{m}$

$$R = \rho \frac{L}{A} = \frac{1 \Omega \text{cm}}{240} \frac{2 \mu\text{m}}{(0.25 \mu\text{m})(0.12 \mu\text{m})} \frac{10,000 \mu\text{m}}{1 \text{cm}} = 2.8 \text{ k}\Omega$$


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Lecture 5: What have we learned?

- Define “extrinsic silicon”
- What are donors and acceptors?
- Why must the impurities be incorporated into the crystal lattice before they can act as dopants?
- Understand how to use charge balance and mass action equations to determine n and p for different doping levels
- Know how to calculate the conductivity of a semiconductor, and the resistance of a bar

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