


CHE323/CHE384  
Chemical Processes for Micro- and Nanofabrication  
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## Lecture 65

# Line-Edge Roughness, part 1

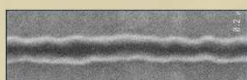
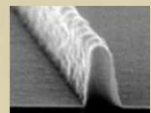
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## What is LER?

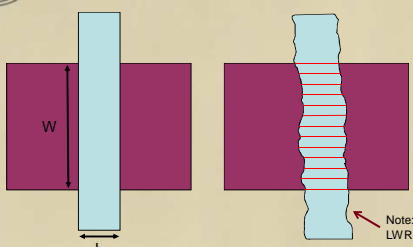
- Line-edge roughness (LER)** - The deviation of a feature edge (as viewed top-down) from a smooth, ideal shape. That is, random (stochastic) edge deviations of a feature.

From: Chris A. Mack, *Fundamental Principles of Optical Lithography: The Science of Microfabrication*, John Wiley & Sons, (London: 2007).

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## Simple Device Model for LER



Note: we often talk about LWR (linewidth roughness)

Break the transistor into many small 1D devices of different lengths, then sum up their currents to get the full device current.  
Result: 1) increased leakage current for the rough gate  
2) average CD error affects transistor speed/leakage

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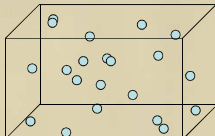
## Continuum Approximation

- The real world is discrete (photons, atoms, etc.), but most macroscopic models (e.g., litho simulation) make the *continuum approximation*
  - Matter and energy are described with continuous mathematical functions
  - Ex: aerial image intensity, acid concentration after exposure, resist dissolution
- What are the implications of making the continuum approximation?
  - Line-edge roughness cannot be predicted

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## Continuum Approximation: Chemical Concentration

- Concentration:** The number of atoms or molecules of a certain type per unit volume
  - By necessity, an average over a volume
- What is the meaning of  $H(x,y,z)$  – the concentration of acid at a specific point in space?



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## Stochastic View of Chemical Concentration

- Model atom/molecule as a point located at its center of mass
- Consider a volume  $V$  – is the molecule in the volume or not?
  - This is a binary proposition, governed by the binomial distribution:  
 $P(n)$  = probability of finding  $n$  molecules in  $V$

$$P(n) = \binom{N}{n} (CdV)^n (1 - CdV)^{N-n} = \frac{N!}{(N-n)!n!} (CdV)^n (1 - CdV)^{N-n}$$

$N = V/dV$ ,  $C$  = average number of molecules per unit volume

- These statistics do not apply if the concentration is very high (atom is not a point), or if there are intermolecular interactions that affect position (e.g., agglomeration)

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### Stochastic View of Chemical Concentration

- The binomial probability distribution can be well approximated a Poisson distribution

$$P(n) = \frac{(CV)^n}{n!} e^{-CV}$$

$$\langle n \rangle = CV \quad \sigma_n^2 = CV$$

$$\frac{\sigma_n}{\langle n \rangle} = \frac{1}{\sqrt{\langle n \rangle}} = \frac{1}{\sqrt{CV}}$$

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### Stochastic View of Chemical Concentration

- Also, if  $CV > 20$ , the Poisson probability distribution can be well approximated a Gaussian distribution

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### Stochastic View of Chemical Concentration

- Example: for a typical 193nm resist formulation,  $G_0 N_A = 0.042 / \text{nm}^3$  ( $G_0$  = the initial concentration of PAG,  $N_A$  = Avogadro's number)

For $V = (3 \text{ nm})^3$	$\langle n \rangle = 1.13$	$\sigma_n / \langle n \rangle = 94\%$
For $V = (6 \text{ nm})^3$	$\langle n \rangle = 9$	$\sigma_n / \langle n \rangle = 33\%$
For $V = (10 \text{ nm})^3$	$\langle n \rangle = 42$	$\sigma_n / \langle n \rangle = 15\%$

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### Photon Shot Noise (Also Poisson)

- Example: for a typical 193nm resist with 10 mJ/cm<sup>2</sup> dose to clear,

For $A = (1 \text{ nm})^2$	$\langle n \rangle = 97$	$\sigma_n / \langle n \rangle = 10\%$
For $A = (10 \text{ nm})^2$	$\langle n \rangle = 9700$	$\sigma_n / \langle n \rangle = 1\%$

- Example: for an EUV resist with 5 mJ/cm<sup>2</sup> dose to clear,

For $A = (1 \text{ nm})^2$	$\langle n \rangle = 3$	$\sigma_n / \langle n \rangle = 58\%$
For $A = (10 \text{ nm})^2$	$\langle n \rangle = 300$	$\sigma_n / \langle n \rangle = 6\%$

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### Lecture 65: What have we Learned?

- Define line-edge roughness (LER)
- What is the continuum approximation?
- Photon and concentration shot noise follow what probability distribution?
- How are the mean and variance related for a Poisson distribution?

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